

A-LEVEL **MATHEMATICS**

Mechanics 1B – MM1B Mark scheme

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Version/Stage V1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from aga.org.uk



Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
Α	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
С	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q	Solution	Mark	Total	Comment
				No MR or MC in this
				question.
1(a)	$v = 14 + 0.8 \times 12$	M1A1		M1: Using constant
	$= 23.6 \mathrm{ms^{-1}}$			acceleration equation(s)
	25.6 m s	A1	3	to find v.
				A1: Correct equation for
				V.
				A1: Correct answer.
				NMS – Full marks for
				correct answer.
				Do not accept 24.
(b)	14 12 1 00 122	M1A1		M1: Using a constant
	$s = 14 \times 12 + \frac{1}{2} \times 0.8 \times 12^2$			acceleration equation or
	$= 225.6 = 226 \mathrm{m} (\mathrm{to}3\mathrm{sf})$	A1		area under a velocity-
	, , ,		3	time graph to find s.
	OR 1	0.61.4.150		A1(F): Correct equation
	$s = \frac{1}{2}(14 + 23.6) \times 12$	(M1A1F)		using their answer to
	2	(A1)	(2)	part (a) if their equation contains v.
	= 225.6 = 226 m (to 3 sf)	(A1)	(3)	A1: Correct answer.
	OR			Accept 225.6 or 226
	23 6 12 1 10 8 12 2	(M1A1F)		7 recept 223.0 of 220
	$s = 23.6 \times 12 - \frac{1}{2} \times 0.8 \times 12^2$	(======)		Do not accept 225
	= 225.6 = 226 m (to 3 sf)	(A1)	(3)	unless 225.6 seen first.
	OR			
		(M1A1F)		Do not accept 230.
	$23.6^2 = 14^2 + 2 \times 0.8s$			
	s = 225.6 = 226 m (to 3 sf)	(A1)	(3)	
(c)	$1600 - R = 1400 \times 0.8$	M1A1		M1: Three term
	R = 480 N			equation of motion with
		A1	3	correct terms. Allow
				sign errors.
				A1: Correct equation. A1: Correct <i>R</i> . CAO
				A1: Correct K. CAO
				NMS – Full marks for
				correct answer.
				Tolloot allo mor.
	T	otal	9	
	·	· 1		1

Q	Solution	Mark	Total	Comment
				No MR or MC in this question.
2(a)	$F = \sqrt{60^2 + 40^2}$	M1	2	M1: Equation or expression to find F or F^2 based on Pythagoras. Must have a +.
	$=\sqrt{5200}$	A1	2	A1: Correct force. Accept AWRT 72.1.
	$= 72.1 \mathrm{N}$			Accept $20\sqrt{13}$. Do not accept 72.
				Note that just $F^2 = 60^2 + 40^2$
	Alternative if angle found first.			Scores M1A0.
	$F = \frac{40}{\sin 33.69^{\circ}} = 72.1$	(M1)		M1:Using 40 and sin of their angle OR 60
	OR	(A1)		and cos of their angle. A1: Correct force. Accept AWRT 72.1.
	$F = \frac{60}{\cos 33.69^{\circ}} = 72.1$	(M1)		A1. Confect force. Accept AWK1 72.1.
	cos 33.69°	$(\mathbf{M}1)$ $(\mathbf{A}1)$		Do not accept 72.
		,		
(b)	$(F\sin\theta = 40)$			
	$(F\cos\theta = 60)$	M1A1		M1: Seeing tan with 40 and 60. can be upside down.
	$\left(\frac{F\sin\theta}{F\cos\theta}\right) = \tan\theta = \frac{40}{60}$	A1	3	A1: Correct expression for tan θ .
	$(F\cos\theta)$ 60 $\theta = 33.7^{\circ}$	711		A1: Correct angle. Accept 33.6 or AWRT
	0 – 33.1			33.7.
	Or	(M1) (A1F)		Do not accept 34°.
	40	(AIF)		M1. Here of all reside 40 and 60 in the
	$\sin\theta = \frac{40}{\sqrt{5200}}$	(A1)	(3)	M1: Use of sin with 40 or 60 in the numerator and their answer to (a) as the
	$\theta = 33.7^{\circ}$			denominator.
	0 – 33.7			A1F: Use of sin and 40 in numerator, provided expression satisfies
	Or	(M1)		$-1 \le \sin \theta \le 1.$
		(A1F)		A1: Correct angle. Accept 33.6 or AWRT
	$\cos\theta = \frac{60}{\sqrt{5200}}$	(A1)		33.7.
	$\sqrt{5200}$ $\theta = 33.7^{\circ}$	(A1)	(3)	M1: Use of cos with 40 or 60 in the
	$\theta = 33.7^{\circ}$			numerator and their answer to (a) as the denominator.
				A1F: Use of cos and 60 in the numerator,
				provided expression satisfies
				$-1 \le \cos \theta \le 1$. A1: Correct angle.
				The Control angle.
				Note that a final answer of 56.3° scores
				M1A0A0.
				Accept answers in radians (0.588).
	Total		5	1

Q	Solution	Mark	Total	Comment
				No MR or MC in this question.
3(a)	$v^{2} = 0^{2} + 2 \times 0.05 \times 6$ $v = 0.775 \text{ m s}^{-1}$ $R_{1} \text{ or } R \text{ or } N_{1}$	M1A1	3	M1: Using constant acceleration equation(s) to find v , with $u = 0$. A1: Correct equation. A1: Correct answer. Accept 0.774 or AWRT 0.775 or $\frac{\sqrt{15}}{5}$ Do not accept 0.77 unless AWRT 0.775 seen first.
(b)	F or μR_1 or $0.4 R_1$ or 3136			Note that if using two equations the time is 15.49s. B1: Correct diagram with exactly four
	mg or $800g$ or W_1 or 7840			forces showing arrow heads and labelled. Note: Do not accept 800 kg for the weight.
		B1	1	
(c)	R_2 or S or N_2 T P Mg or $1700g$ or W_2 or 16660	B1		B1: Correct diagram with exactly four forces showing arrow heads and labelled. Do not award if a different letter is used for the tension in this part. Condone the use of the same letter for the normal reaction and the weight / mass in both parts. Condone assumption that normal reaction is equal to the weight when labelling diagrams. Condone diagrams with two or four normal reactions if they are seen acting at the wheels. Note: Do not accept 1700 kg for the weight.
	Only one normal reaction force / Don't need to consider where the normal reaction forces act.	B1	2	B1: Any comment about the number of normal reaction forces or where they act.
(d)	$R = 800 \times 9.8$ $(= 7840 \text{ N})$ $F = 0.4 \times 800 \times 9.8$ $= 3136 = 3140 \text{ N (to 3sf)}$	M1 dM1 A1	3	M1: Correct reaction force. dM1: Use of $F = \mu R$. Accept $800g$ for R . Condone negative signs in working. A1: Correct friction. Only accept 3140 or 3136. Do not award for negative final answers.

Q	Solution	Mark	Total	Comment
(e)	$T - 3136 = 800 \times 0.05$ T = 3176 = 3180 N (to 3 sf)	M1A1F A1	3	M1: Three term equation of motion for the skip with correct terms. Allow sign errors and their value of <i>F</i> from part (d). Must use mass of 800 kg. A1F: Correct equation with their value for <i>F</i> . A1: Correct <i>T</i> . Only accept 3176 or 3180.
(f)	$P-3176 = 1700 \times 0.05$ P = 3261 = 3260 N (to 3sf) OR $P-3136 = 2500 \times 0.05$	M1A1F A1 (M1A1F)	3	M1: Three term equation of motion for the van with correct terms. Allow sign errors and their value of <i>T</i> from part (e). Must use mass of 1700 kg. A1F: Correct equation. Follow through their value for <i>T</i> . A1: Correct <i>P</i> . Accept 3261.
	P = 3261 = 3260 N (to 3sf)	(A1)	(3)	Allow 3265 or 3260 or 3270 from use of 3180 for <i>T</i> . M1: Three term equation of motion for the van and skip with correct terms. Allow sign errors and their value of <i>F</i> from part (d). Must use mass of 2500 kg. A1F: Correct equation. Follow through their value for <i>F</i> . A1: Correct <i>P</i> . Accept 3261. Allow 3265 or 3260 or 3270 from use of
	Tota	1	15	3140 for <i>F</i> . Use of <i>g</i> = 9.81 gives: (d) 3139.2 (e) 3179.2 (f) 3264.2
				Do not penalise use of 9.81.

Q	Solution	Mark	Total	Comment
				No MR or MC in this question.
4(a)	$t = \frac{20}{2\sin 70^{\circ}}$ $= 10.6 \text{ seconds}$	M1A1	2	M1: Use of distance divided by speed (20 ÷ 2sin70° or 2cos70° or 2sin20° or 2cos20°
	To to seconds	A1	3	OR $ \sqrt{409} \div \frac{2\sin 70^{\circ}}{\sin \alpha} $ Value for α does not have to be seen. A1: Correct expression for t , with $\alpha = 81.5$ if included. A1: Correct time. Accept AWRT 10.6.
(b)	$\tan\alpha = \frac{20}{3}$	M1		M1: Use of $\tan \alpha = \frac{20}{3}$ or $\frac{3}{20}$. Allow use
	$\alpha = 81.5$	A1	2	of sin or cos with $\sqrt{409}$ in the denominator. A1: Correct angle. Allow AWRT 81.5 or 81, but not 81.0.
(c)	$180 - 70 - 81.46 = 28.53$ $\frac{V}{\sin 28.53^{\circ}} = \frac{2}{\sin 81.47^{\circ}}$ $2\sin 28.53^{\circ}$	M1A1 A1		M1: Forming an equation to find <i>V</i> . A1, A1: Correct equation award A2, if one error award A1. dM1: Solving equation for <i>V</i> A1: Correct <i>V</i> . Accept AWRT 0.97 from
	$V = \frac{2\sin 28.53^{\circ}}{\sin 81.47^{\circ}} = 0.966$ OR	dM1A1	5	correct working, particularly from working with 10.6 or 8.5° etc.
	$(V - 2\cos 70^{\circ}) \times 10.64 = 3$ V = 0.966 OR	(M1A1) (A1) (dM1A1)		
	$20 \tan 20^{\circ} + 3 = 10.64V$ V = 0.966 OR	(M1A1) (A1) (dM1A1)		
	$V = 2\cos 70^{\circ} + 2\sin 70^{\circ} \tan 8.53^{\circ}$ $= 0.966$	(M1A1) (A1) (dM1A1)		
		Total	10	

Q	Solution	Mark	Total	Comment
				Follow through
				mis-reads in this question.
5	$m(4\mathbf{i} + 2\mathbf{j}) + km(6\mathbf{i} - 2\mathbf{j}) = (m + km)(5.2\mathbf{i} - 0.4\mathbf{j})$	B1		B1: Correct vector
	4m + 6km = 5.2(m + km)	21		equation for
		M1A1		conservation of
	4 + 6k = 5.2 + 5.2k			momentum. Can be
	0.8k = 1.2	dM1		implied in later working by correct equation for
	$k = \frac{1.2}{0.8} = 1.5$	A1	5	one component.
	$\kappa = \frac{1.5}{0.8}$			Condone missing
	OR			brackets if later working
	2m - 2km = -0.4(m + km)	(M1A1)		correct.
	2 - 2k = -0.4 - 0.4k			M1: Conservation of
	2.4 = 1.6k	(dM1)		momentum equation for one component with
	2.4	(A1)		correct terms, but allow
	$k = \frac{2.4}{1.6} = 1.5$, ,		sign errors.
	1.0			A1: Correct equation.
				Allow inclusion of i or j
				in equations. dM1: Valid method for
				solving for k .
				Working like $k = \frac{1.2i}{0.8i} = 1.5$
				scores dM0.
				A1: Correct value for <i>k</i> .
				CAO
				Candidates who work
				with both components
				and get two different
				values for k, should be
				treated as two solutions.
				(Mark both and take mean, rounding down.)
				mean, rounding down.)
	OR			M1: Forming aquation
	$-1.2\mathbf{i} + 2.4\mathbf{j} = k(-0.8\mathbf{i} + 1.6\mathbf{j})$	(M1A1)		M1: Forming equation for <i>k</i> using magnitudes
	$1.2^2 + 2.4^2 = k^2(0.8^2 + 1.6^2)$			of vectors.
	$k^2 = \frac{7.2}{3.2}$			A1: Correct equation.
	3.2 $k = \pm 1.5$	(dM1)		dM1: Obtaining ±1.5
	$k = \pm 1.5$ $k = 1.5$			A1: Selecting 1.5.
		(A1)		Consistent use of weight
				instead of mass deduct 1
				mark.
	Total		5	

Q	Solution	Mark	Total	Comment
				No MR or MC in this question.
6(a)	$V\cos 2^{\circ} \times 1.8 = 420$	M1A1		M1: Equation to find <i>V</i> with
	$V = \frac{420}{1.8\cos 2^{\circ}} = 233.47 = 233 \mathrm{m s^{-1}} \text{ (to 3sf)}$	A1	3	420 = V × 1.8 (cos2° or sin2°). A1: Correct equation. A1: Correct V. Allow 233.5 or AWRT233 from correct working.
(b)	$y = 233.47 \sin 2^{\circ} \times 1.8 - \frac{1}{2} \times 9.8 \times 1.8^{2}$ $= -1.209 = -1.21 \text{ m (to 3sf)}$	M1A1F A1		M1: Use of constant acceleration equation to find y (vertical displacement). Allow cos2° and ±g. A1F: Correct equation. Follow
	Distance between A and C is 1.21 metres.	A1	4	through their <i>V</i> from part (a). A1: Correct <i>y</i> . Accept AWRT -1.21. Accept-1.23 or -1.24 from use of 233, provided correct working seen in part (a). Accept-1.20 or -1.21 from use of 233.5, provided correct working seen in part (a).
(-)	Na sin nasiatan sa	D1	1	A1: Correct distance. Accept modulus of answers as above.
(c)	No air resistance.	B1	1	B1: No (air) resistance or only force is weight. Do not allow 'only force acting is g'.
	Total	-	8	
				Use of <i>g</i> = 9.81 gives: (b) -1.2258 Use of 233 gives -1.2555. Use of 233.5 gives -1.2239. Do not penalise use of 9.81.

Q	Solution	Mark	Total	Comment
				Candidates who use
				a = -0.4i + 0.2j for both
				particles can gain all method
				marks but no A or B marks.
				Otherwise no MR or MC in
7(0)				this question.
7(a)	$\mathbf{r} = (4\mathbf{i} + 2\mathbf{j}) \times 10 + \frac{1}{2}(-0.4\mathbf{i}) \times 10^{2}$	M1		M1: Use of $\mathbf{u}t + \frac{1}{2}\mathbf{a}t^2$ with a
	$=20\mathbf{i}+20\mathbf{j}$	A1	2	non-zero acceleration. A1: Correct position vector.
(b)	$\mathbf{r}_A = (4\mathbf{i} + 2\mathbf{j})t - 0.2t^2\mathbf{i}$	B1		B1: Seeing position vector for
				A, may be implied by later
	$\mathbf{r}_B = (0.4\mathbf{i} + 0.6\mathbf{j})t + 0.1t^2\mathbf{j} + 11.2\mathbf{i}$	B1		working if not seen explicitly.
	$(4\mathbf{i} + 2\mathbf{j})t - 0.2t^2\mathbf{i} = (0.4\mathbf{i} + 0.6\mathbf{j})t + 0.1t^2\mathbf{j} + 11.2\mathbf{i}$			B1: Seeing position vector for
	$2t = 0.6t + 0.1t^2$	M1A1		B, may be implied by later
		WITAT		working if not seen explicitly. M1: Forming an equation by
	$t^2 - 14t = 0$			equating either i or j
	(t = 0) or $t = 14$	A1		components to form a
				quadratic equation.
	$4t - 0.2t^2 = 0.4t + 11.2$	dM1A1		A1: Correct equation
	$t^2 - 18t + 56 = 0$			A1: Correct solution(s).
				dM1: Forming an equation by
	t = 4 or $t = 14$	A1		equating other components to
	$\therefore t = 14$	Al		form a quadratic equation. A1: Correct equation
	OR			A1: Correct solutions and
	$4 \times 14 - 0.2 \times 14^2 = 16.8$	(dM1)		selection of common solution.
		(A1)		
	$0.4 \times 14 + 11.2 = 16.8$			(dM1): Substituting one non-
		(A1)		zero value from their two
	$\therefore t = 14$			solutions into the other
	THEN			component for both A and B.
	ITEN			(A1): Obtaining two identical values.
				(A1):Concluding that $t = 14$.
	$\mathbf{r} = (4\mathbf{i} + 2\mathbf{j}) \times 14 - 0.2 \times 14^2 \mathbf{i} = 16.8\mathbf{i} + 28\mathbf{j}$			(111). Concluding that t = 14.
	$\mathbf{i} = (\pi \mathbf{i} + 2\mathbf{j}) \wedge \mathbf{i} + 0.2 \wedge \mathbf{i} + \mathbf{i} = 10.0\mathbf{i} + 20\mathbf{j}$	B1	9	B1: Correct position vector.
	Total		11	

Q	Solution	Mark	Total	Comment
				No MR or MC in this
				question.
8(a)	$F = 40 \times 9.8 \sin 30^\circ = 196 \text{ or } F = mg \sin 30^\circ$	M1A1		M1: Resolving parallel and
	$R = 40 \times 9.8 \cos 30^{\circ} = 339.48$ or $R = mg \cos 30^{\circ}$	A1		perpendicular to the slope to obtain expressions for <i>F</i> and <i>R</i> .
	$40 \times 9.8 \sin 30^{\circ} = \mu \times 40 \times 9.8 \cos 30^{\circ}$	dM1		Allow consistent mixing of sin
		GIVII		and cos.
	$\mu = \frac{\sin 30^{\circ}}{\cos 30^{\circ}} = \tan 30^{\circ} = 0.577$			A1: Correct <i>F</i> .
		A 1	5	A1: Correct R.
	OR			dM1: Use of $F = \mu R$
	$\mu = \frac{196}{339.48} = 0.577$			A1: Correct μ . Accept $\frac{1}{\sqrt{3}}$ or
				$\frac{\sqrt{3}}{3}$ or AWRT 0.577
				or AWRT 0.578.
				NMS gives full marks.
				Complete solution with omission of <i>g</i> throughout with
				correct final answer scores SC4.
(b)(i)	$R = X \sin 30^{\circ} + 40 \times 9.8 \cos 30^{\circ}$	M1A1		M1: Resolving perpendicular to
			2	the plane with three terms; R ,
	(=0.5X+339.5)			Xsin30° or Xcos30° and
				40gcos30° or 40gsin30°, with
				consistent mixing of sin and
				cos. Allow sign errors. A1: Correct expression for <i>R</i> ,
				may include m and g .
(b)(ii)	$X \cos 30^{\circ} - 40 \times 9.8 \sin 30^{\circ} - F = 40 \times 0.2$	M1A1		M1: Equation of motion with
				correct terms. Allow sign
				errors.
				A1: Correct equation. May be
				in terms of m and g .
	$X \cos 30^{\circ} - 196 - \tan 30^{\circ} (0.5X + 392 \cos 30^{\circ}) = 8$	dM1		dM1: Substituting for F using $F = \mu R$, where R is in the form
	A cos 30 170 tail 30 (0.3A + 372 cos 30) = 0	GIVII		a + bX where a and b are non-
	9 + 106 + 202 and 20° top 20°			a + bA where a and b are non- zero constants.
	$X = \frac{8 + 196 + 392\cos 30^{\circ} \tan 30^{\circ}}{\cos 30^{\circ} - 0.5 \tan 30^{\circ}} = 692.8 = 693 \text{ N (to 3sf)}$	dM1	5	dM1: Solving for X.
	C0330 0.3 tail 30	A1		A1: Correct value for <i>X</i> . Accept
				692 or AWRT 693.
	Alternative format			
	$X\cos 30^{\circ} - 40g\sin 30^{\circ} - F = 40 \times 0.2$			
	$X\cos 30^{\circ} - 40g\sin 30^{\circ} - \tan 30^{\circ}(0.5X + 40g\cos 30^{\circ}) = 8$			
	$X = \frac{8 + 40g\sin 30^\circ + 40g\cos 30^\circ \tan 30^\circ}{\cos 30^\circ - 0.5\tan 30^\circ} = 692.8 = 693 \text{ N (to 3sf)}$			
	$\cos 30^{\circ} - 0.5 \tan 30^{\circ}$			
	Total		12	
	TOTAL		75	
				Use of $g = 9.81$ gives:
				(b) (i) $0.5X + 339.8$
				(b) (ii) 693.5 = 694 (to 3sf)
				Do not penalise use of 9.81.