

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										



General Certificate of Education
Advanced Subsidiary Examination
January 2011

Mathematics

MPC1

Unit Pure Core 1

Monday 10 January 2011 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.
- You must **not** use a calculator.



Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The use of calculators is **not** permitted.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
TOTAL	



J A N 1 1 M P C 1 0 1

Answer **all** questions in the spaces provided.

- 1** The curve with equation $y = 13 + 18x + 3x^2 - 4x^3$ passes through the point P where $x = -1$.
- (a) Find $\frac{dy}{dx}$. (3 marks)
- (b) Show that the point P is a stationary point of the curve and find the other value of x where the curve has a stationary point. (3 marks)
- (c) (i) Find the value of $\frac{d^2y}{dx^2}$ at the point P . (3 marks)
- (ii) Hence, or otherwise, determine whether P is a maximum point or a minimum point. (1 mark)

QUESTION
PART
REFERENCE



QUESTION
PART
REFERENCE

Turn over ►



(1 mark)

(b) Express $\frac{4\sqrt{3} + 3\sqrt{7}}{3\sqrt{3} + \sqrt{7}}$ in the form $\frac{m + \sqrt{21}}{n}$, where m and n are integers. (4 marks)

This image shows a blank sheet of white paper designed for handwriting practice. It features a solid black vertical line on the left side, creating a narrow margin. The rest of the page is filled with evenly spaced, horizontal dashed lines for writing. There are no other markings, text, or illustrations on the page.



QUESTION
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REFERENCE

Turn over ►



- 3** The line AB has equation $3x + 2y = 7$. The point C has coordinates $(2, -7)$.
- (a) (i)** Find the gradient of AB . (2 marks)
- (ii)** The line which passes through C and which is parallel to AB crosses the y -axis at the point D . Find the y -coordinate of D . (3 marks)
- (b)** The line with equation $y = 1 - 4x$ intersects the line AB at the point A . Find the coordinates of A . (3 marks)
- (c)** The point E has coordinates $(5, k)$. Given that CE has length 5, find the two possible values of the constant k . (3 marks)

QUESTION
PART
REFERENCE



QUESTION
PART
REFERENCE

Turn over ►



QUESTION
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Turn over ►



A Cartesian coordinate system with x and y axes. The origin is labeled O. A parabola opens downwards, with its vertex in the second quadrant. A line segment connects point A on the x-axis at x = -2 to point P(1, 12) on the parabola. The region bounded by the parabola, the line segment AP, and the x-axis is shaded gray. The x-axis is labeled with -2 and 1.

(ii) Hence find the area of the shaded region bounded by the curve $y = 14 - x - x^4$ and the line AP . (2 marks)

QUESTION	PART	REFERENCE
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QUESTION
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REFERENCE

Turn over ►



[illegible]

[illegible]

5 (a) (i) Sketch the curve with equation $y = x(x - 2)^2$. (3 marks)

(ii) Show that the equation $x(x - 2)^2 = 3$ can be expressed as

$$x^3 - 4x^2 + 4x - 3 = 0 \quad (1 \text{ mark})$$

(b) The polynomial $p(x)$ is given by $p(x) = x^3 - 4x^2 + 4x - 3$.

(i) Find the remainder when $p(x)$ is divided by $x + 1$. (2 marks)

(ii) Use the Factor Theorem to show that $x - 3$ is a factor of $p(x)$. (2 marks)

(iii) Express $p(x)$ in the form $(x - 3)(x^2 + bx + c)$, where b and c are integers. (2 marks)

(c) Hence show that the equation $x(x - 2)^2 = 3$ has only one real root and state the value of this root. (3 marks)

QUESTION
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[illegible]

[illegible]

[illegible]

(iii) Hence find an equation of the tangent to the circle at the point D . (2 marks)

[illegible]

[illegible]

[illegible]

[illegible]

7 (a) (i) Express $4 - 10x - x^2$ in the form $p - (x + q)^2$. (2 marks)

(ii) Hence write down the equation of the line of symmetry of the curve with equation $y = 4 - 10x - x^2$. (1 mark)

(b) The curve C has equation $y = 4 - 10x - x^2$ and the line L has equation $y = k(4x - 13)$, where k is a constant.

(i) Show that the x -coordinates of any points of intersection of the curve C with the line L satisfy the equation

$$x^2 + 2(2k + 5)x - (13k + 4) = 0 \quad (1 \text{ mark})$$

(ii) Given that the curve C and the line L intersect in two distinct points, show that

$$4k^2 + 33k + 29 > 0 \quad (3 \text{ marks})$$

(iii) Solve the inequality $4k^2 + 33k + 29 > 0$. (4 marks)

QUESTION
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REFERENCE



[illegible]

QUESTION
PART
REFERENCE**END OF QUESTIONS**

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