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Other Names					
Candidate Signature					



General Certificate of Education Advanced Subsidiary Examination January 2011

# **Mathematics**

MPC1

**Unit Pure Core 1** 

Monday 10 January 2011 9.00 am to 10.30 am

### For this paper you must have:

• the blue AQA booklet of formulae and statistical tables. You must **not** use a calculator.



# Examiner's Initials Question Mark 1 2 3 4 5 6 7 TOTAL

### Time allowed

• 1 hour 30 minutes

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The use of calculators is **not** permitted.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

### **Advice**

 Unless stated otherwise, you may quote formulae, without proof, from the booklet.



## Answer all questions in the spaces provided.

- The curve with equation  $y = 13 + 18x + 3x^2 4x^3$  passes through the point P where x = -1.
  - (a) Find  $\frac{dy}{dx}$ . (3 marks)
  - Show that the point P is a stationary point of the curve and find the other value of x where the curve has a stationary point. (3 marks)
  - (c) (i) Find the value of  $\frac{d^2y}{dx^2}$  at the point P. (3 marks)
    - (ii) Hence, or otherwise, determine whether P is a maximum point or a minimum point. (1 mark)

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2 (a	) Simplify	$(3\sqrt{3})^2$ .						(1 mark)
(b	) Express	$\frac{4\sqrt{3}+3\sqrt{7}}{3\sqrt{3}+\sqrt{7}}$	in the form	$\frac{m+\sqrt{21}}{n},$	, where <i>m</i>	and <i>n</i> are in	ntegers.	(4 marks)
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3		The line AB has equation $3x + 2y = 7$ . The point C has coordinates $(2, -7)$ .
(a	) (i)	Find the gradient of AB. (2 marks)
	(ii)	The line which passes through $C$ and which is parallel to $AB$ crosses the $y$ -axis at the point $D$ . Find the $y$ -coordinate of $D$ . (3 marks)
(b	)	The line with equation $y = 1 - 4x$ intersects the line AB at the point A. Find the coordinates of A. (3 marks)
(с	)	The point $E$ has coordinates $(5, k)$ . Given that $CE$ has length 5, find the two possible values of the constant $k$ . (3 marks)
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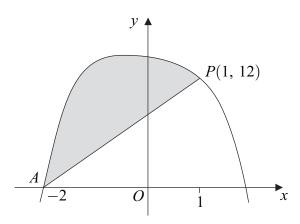
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**4** The curve sketched below passes through the point A(-2, 0).



The curve has equation  $y = 14 - x - x^4$  and the point P(1, 12) lies on the curve.

- (a) (i) Find the gradient of the curve at the point P. (3 marks)
  - (ii) Hence find the equation of the tangent to the curve at the point P, giving your answer in the form y = mx + c. (2 marks)

**(b) (i)** Find 
$$\int_{-2}^{1} (14 - x - x^4) dx$$
. (5 marks)

(ii) Hence find the area of the shaded region bounded by the curve  $y = 14 - x - x^4$  and the line AP.

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- **5 (a) (i)** Sketch the curve with equation  $y = x(x-2)^2$ . (3 marks)
  - (ii) Show that the equation  $x(x-2)^2 = 3$  can be expressed as

$$x^3 - 4x^2 + 4x - 3 = 0 (1 mark)$$

- **(b)** The polynomial p(x) is given by  $p(x) = x^3 4x^2 + 4x 3$ .
  - (i) Find the remainder when p(x) is divided by x + 1. (2 marks)
  - (ii) Use the Factor Theorem to show that x 3 is a factor of p(x). (2 marks)
  - (iii) Express p(x) in the form  $(x-3)(x^2+bx+c)$ , where b and c are integers. (2 marks)
- Hence show that the equation  $x(x-2)^2 = 3$  has only one real root and state the value of this root. (3 marks)

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6		A circle has centre $C(-3, 1)$ and radius $\sqrt{13}$ .	
(а	) (i)	Express the equation of the circle in the form	
		$(x-a)^2 + (y-b)^2 = k$	(2 marks)
	(ii)	Hence find the equation of the circle in the form	
		$x^2 + y^2 + mx + ny + p = 0$	
		where $m$ , $n$ and $p$ are integers.	(3 marks)
(b	)	The circle cuts the y-axis at the points $A$ and $B$ . Find the distance $AB$ .	(3 marks)
(с	) (i)	Verify that the point $D(-5, -2)$ lies on the circle.	(1 mark)
	(ii)	Find the gradient of CD.	(2 marks)
	(iii)	Hence find an equation of the tangent to the circle at the point $D$ .	(2 marks)
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- **7 (a) (i)** Express  $4 10x x^2$  in the form  $p (x + q)^2$ . (2 marks)
  - (ii) Hence write down the equation of the line of symmetry of the curve with equation  $y = 4 10x x^2$ . (1 mark)
  - (b) The curve C has equation  $y = 4 10x x^2$  and the line L has equation y = k(4x 13), where k is a constant.
    - (i) Show that the x-coordinates of any points of intersection of the curve C with the line L satisfy the equation

$$x^{2} + 2(2k+5)x - (13k+4) = 0 (1 mark)$$

(ii) Given that the curve C and the line L intersect in two distinct points, show that

$$4k^2 + 33k + 29 > 0 (3 marks)$$

(iii) Solve the inequality  $4k^2 + 33k + 29 > 0$ . (4 marks)

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