

A-LEVEL **Mathematics**

MD02 - Decision 2

Mark scheme

6360

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the relevant

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
Α	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
−x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
С	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

								4thsc/o,
1			Solution			Mark	Total	Comment
1)	6	11	7	2	**	B1		All alamants & raplaced
	10	6	1	0	**	В		All elements x replaced with $k - x$, $k \ge 19$
	9 5	8 7	6 2	8	**			$\sqrt{n} = \sqrt{n}$
	8	10	5	5	**	B1	2	Extra column introduced
	0	10	3	3				with all values being the same non-negative number may be seen in (b)
)	1	5	6	2	0			
	5	0	0	0		M1		Column reduction with 4
	4	2	5	8	0			or more columns correct
-	3	1	1	10 5		A1		All columns correct and
	3	4	4	3	φ			three lines used to cover zeros (may have vertical line in 1 st col, see alt)
			~					Accompanies (by 1) with
	0	4	5	1 0	0	dM1		Augmenting (by 1) with 4 or more rows/columns
	3	1	4	7				correct
	0	1	1	10				A.I
	2	3	3	4	ф	A1		All correct with three lines drawn to cover zeros
	0* 6 3 0	3 0 0* 0 2	4 0 3 0* 2	0 0* 6 9	0 2 0 0 0 1 0 1 0 1 1 1 1 1 1 1 1 1 1 1	dM1		Augmenting (by 1) with 4 or more rows/columns correct
	ve lines nee ocation four		er the zer	os, so opti	mal	A1		All correct with five lines drawn to cover zeros and 'optimal' seen

Notes: Candidate may write answer to (a) in (b), do not penalise, give benefit of doubt to candidate **(b)** need to see (at least) 'optimal' for **A1** Statement about Tom needs to be in context, not just 'Tom'

	Solution	Mark	Total	Comment
)	Alternative	IVIAIN	TOtal	Comment
,				
	5 6 2 0	M1		Column reduction with 1
	5 0 0 0	IVI I		Column reduction with 4 or more columns correct
	4 2 5 8 0			or more columns correct
	0 1 1 10 0 3 4 4 5 0	A1		All columns correct and
				three lines used to cover zeros
				25.55
	1 4 5 1 0			Augmenting (by 1) with
	6 0 0	dM1		4 or more rows/columns
	4 1 4 7 0			correct
	0 0 9	A1		All correct with three
	3 3 3 4 0			lines drawn to cover
	·			zeros
	0* 3 4 0 0	4884		Augmenting (by 1) with 4
	6 0 0 0* 2	dM1		or more rows/columns correct
	3 0* 3 6 0			Correct
	2 2 2 3 0*			
	Five lines needed to cover the zeros, so optimal	A1		All correct with five lines
	allocation found			drawn to cover zeros

								Comment
Q2			Solutio	on		Mark	Total	Comment
a) (i)	[18 + 20 + 25 + 87] = 150					B1		
a) (ii)	[51 + 1	4 - 5 - 3 + 8	37] = 144			B1	2	
(b) [[Max] fl	ow ≤ their m	in from (a)			M1		
[[Max] flow of gas [through the network of] pipes must be less than or equal to 144 cm ³ s ⁻¹ OE						2	Including units
(c)(i)		Arc	Forward	Backward		М1		Correct at SA, AC, SB,
		SA	29	0				and BE
		AC	4	0		M1		Compact at CE ET EC
		$\frac{CF}{FT}$	17 68	5				Correct at CF , FT , EG , and GT
		AD	1	6				and of
		DF	6	5		A 1	3	All correct
		DC	15	0				All correct
		DE	8	0				
		$\frac{SB}{BE}$	32 14	3				
		EG	4	10				
		GT	67	0				
		BD	0	4				
		DG	22	2				
->/::>	N 4115 -1		- - - - - - - - - - - - -	L to		D4		
		sing) correct		h increasing and gram		B1		
	e.g.	Death		Farm Fi	\neg	8.64		One compet with a little and
		Path SACFT		Extra Flow 4	\dashv	M1		One correct path and extra flow in table
		SAD(CF, F	F or G)T	1		Αd		
		SBEGT		4		A 1		Two correct paths and extra flows in table
						A 1	4	All correct
o)/iii)	rna	20 : 4	. 1 . 4 . 7 .	17 Fam ³ 13		D4	4	
c)(iii) [lıvıax. fl	ow = 38 + 4	$+1+4=\int_{-2}^{2}$	r/[cm ⁻ s ⁻]		B1	1	

Notes: (b) may see symbols for 'less than or equal to' (c) If M0 scored in (i), then candidate scores B0 in (ii)

(c)(i) if M0M0 scored, SC1 for SA, AC, CF, FT or SB, BE, EG, GT all correct

(c)(ii) there are other obtuse possibilities, but any correct soln must have total(SA...T) = 5 and SBEGT = 4

Note: there is no path SACD...T allowable

				5 - MD02 - JUI Mynathsol
[If John plays] [J ₁] [J ₂]	[Expected gain for Winnie] $0q + (-2)r + 4(1-q-r) [= 4-4q-6r] \\ -2q + 7r + (-6)(1-q-r) [= -6+4q+13r]$	M1		Either expression correct (including the use of exactly two probability variables)
$ \begin{array}{r} 4 - 4q - 6r = -4 \\ -6 + 4q + 13r \end{array} $	-4 / 11 = -4 / 11	A1F		Sets the correct expressions equal to their value of the game from (b)
q = 9/11, r = 2	2/11	A 1		Both values correct
Winnie plays:	 W₁ [with probability] 9/11 W₂ [with probability] 2/11 W₃ [with probability] 0 	E1	4	Must have all three probabilities
Alternative So	olution			
Winnie never $[$ If John plays $]$ $[J_1]$ $[J_2]$	[Expected gain for Winnie] $0p + (-2)(1-p) [= -2 + 2p]$ $-2p + 7(1-p) [= 7 - 9p]$	(M1)		Either expression correct
-2 + 2p = 7 - 9	∂p	(A1)		Sets the correct gain expressions equal to each other
p = 9/11		(A1)		
Winnie plays:	 W₁ [with probability] 9/11 W₂ [with probability] 2/11 W₃ [with probability] 0 	(E1)		Must have all three probabilities, but W ₃ made be stated as never played earlier in the solution

		Solu	Mark	Total	- MD02 - JUI MAITISCIO		
Ctoo	. Ctata	From	Value		,		
Stag	ge State	T	Value	475*	-		
1	J	T		480*	-		
	K	T		475*]		
		7	(470, 475)	47.5*			
2	D E	I I	max(470, 475)	475* 475*	B1		9 Values at Stage 2
	E	J	max(470, 475) max(465, 480)	480	-		
	F	I	max(495, 475)	495			
	I.	J	max(490, 480)	490*	M1		Using minimax –
		K	max(495, 475)	495			choosing at least two of
	G	J	max(485, 480)	485			EI, FJ or GK (PI)
		K	max(480, 475)	480*	A1		All reduces as a second
	Н	K	max(475, 475)	475*	AI		All values correct at Stage 2
3	A	D	max(480, 475)	480*			
		E	max(515, 475)	515]		
		F	max(490, 490)	490	B1		9 Values at Stage 3
	В	E	$\max(485, 475)$	485			
		F	max(475, 490)	490	dM1		At least 7 values correct
	- C	G	max(480, 480)	480*			
	<i>C</i>	F G	max(490, 490) max(500, 480)	490* 500	A1		All values correct at
		H	max(495, 475)	495]		Stage 3
4	S	A	max(465, 480)	480*	B1		3 Values at Stage 4
		В	max(470, 480)	480*	ן יט ון		3 Values at Stage 4
		С	max(460, 490)	490	A1		All values correct at Stage 4
S-B-G-					A 1		One correct route (not reversed)
S-A-D-I	I-T				A1		2 nd correct route (not reversed) AND no others

	0										30
(a)					Solution	nn			Mark	Total	Comment
(b)	a < 0	a < 0						B1	1		
	$\frac{b}{1/2}$ <	$<\frac{c}{3/2}$	<u>-</u>						M1		
:	3 <i>b</i> <	С							A 1	2	NMS 2/2
(c)(i)	d ± 3	× 7,	/2						M1		
d	d + 2	1/2	OI	E					A 1	2	NMS 2/2
(c)(ii)							ı		B1		D 1 x 0 x 0 and
	P	x	у	z	S	t	и	value	ы		P = 1, $x = 0$, $y = 0$ and $u = 0$ all correct
	1	0	0	35 - 7a	-2 <i>a</i>	10 + a	0	100 - 2ab			
									M1		One of z, s or t correct
									A 1		z, s and t all correct
									B1	4	value = 100 – 2 <i>ab</i>
(c)(iii)	10 +	a ≥ (0	OE					M1		their $t \ge 0$ PI by final answer
-	−10 <u>≤</u>	≤ a <	< 0						A 1	2	Allow $-10 \le a$ AND $a < 0$

Notes: (b) For A1, accept $b < \frac{1}{3}c$, or $\frac{1}{3}c > b$ or c > 3b BUT NOT 6b < 2c

(c)(i)(ii) for both parts condone correct multiples for all marks eg d/k + 21/2k

(ii) condone omission of 'heading row', but be convinced

(iii) their $(10 + a) \ge 0$ seen anywhere in soln scores M1

						Comment	640
Q6		Solution	Mark	Total	Comment		
(a)	Activity	Early	Late	B1		All early times correct	
	$\frac{A}{B}$	0	<u>7</u> 6				
	C D	5	15	B1		All late times correct	
	$\frac{D}{E}$	6	14 14				
	F	13	22				
	G H	14 14	22 23				
	I	22	31				
	J	22	31				
	K	31	40		2		
(b)	B-E-G-I-K			B1	1	Or reverse	
(c)				M1		SCA, at least 10 labelle activities	d
	<u></u>	<u>-</u>		B1		Use of floats, at least three of <i>A</i> , <i>C</i> , <i>D</i> , <i>F</i> , <i>H</i> , <i>J</i> (either before or after activity)	
				A1		All correct, including labelling and all floats before activity correct	
	10 20	30	40 50		3		
(i)(k	Reduce G by 5 days	S		E1		Decrease G to 3 days	
	Reduce both F and	H by 3 days		E1		Decrease F and H both to 4 days	
d)(ii)	$(g \times 500) + (f \times 250)$	the minimum compl + $(h \times 650)$ eir f , g , h non-zero)		M1		Calculates cost of reducing durations by 'their' reductions in (d) (i)
	[£]5200			A 1		CAO	
	[£]5200 > [£]5000, (s from the bonus pay	so the company with ment) so don't redu		E1F	5	Comparing their 5200 to 5000 PI and making a correct conclusion about whether to reduce durations	

Notes: (c) For M1 all non-critical activities must be on a separate row (d)(ii) eg if their answer is less than 5000, (the company would benefit from the bonus) so reduce **E1F** Accept: 'Yes/No' plus valid reason in context

				Comment
Q7	Solution	Mark	Total	Comment
(a)	Row Minima = -2 , -5 , -6 , -2 Column Maxima = -2 , 6 , -2 , 7	М1		Finds all row minima or all column maxima (may be seen on table.) Condone one slip
	Max(Row Minima) = -2 Min(Row Maxima) = -2	A 1		Both correct (may be indicated, not stated from 8 correct values)
	Any two of AW, AY, DW and DY stated	A1		
	All four saddle points correct and no others stated	A 1	4	AW, AY, DW and DY.
(b)	Y dominates Z	B1		
	$\operatorname{as} \begin{pmatrix} 2x \\ x-3 \\ -2 \\ -2 \end{pmatrix} < \begin{pmatrix} 3 \\ -5 \\ 7 \\ 6 \end{pmatrix} \text{ for integer } x < -3.$	E1		OE statement with $x < -3$ mentioned/used
	D dominates C	B1 dep		Dependent on first B mark
	as $(x-1 \ 1 \ -2) \ge (x-3 \ 3x-3 \ -2)$ for integer $x < -3$.	E1		OE statement with $x < -3$ mentioned/used
	W (or Y) dominates X	B1 dep		Dependent on first and second B marks, and no other further dominances stated/used
	$\operatorname{as} \begin{pmatrix} -2 \\ -3 \\ x - 1 \end{pmatrix} < \begin{pmatrix} 5 \\ 6 \\ 1 \end{pmatrix} \text{ for integer } x < -3$	E1	6	OE statement with $x < -3$ mentioned/used
	$ \left[or \begin{pmatrix} 2x \\ x-3 \\ -2 \end{pmatrix} < \begin{pmatrix} 5 \\ 6 \\ 3 \end{pmatrix} \right] $			
	Total		10	

Notes: (a) the final A1A1 are independent of previous A1

the 'co-ordinates eg AW' must be stated not merely circling entries in the table for the final A1A1

If M0 scored then SC1 for two or more correct saddle points

(b) working may be seen on table

A candidate may subst x = -4 (instead of x < -3) and consider dominance as above. In this case all marks are available. (possibly by drawing a new amended matrix)

A candidate who subst x = -3 can score the **B** marks only